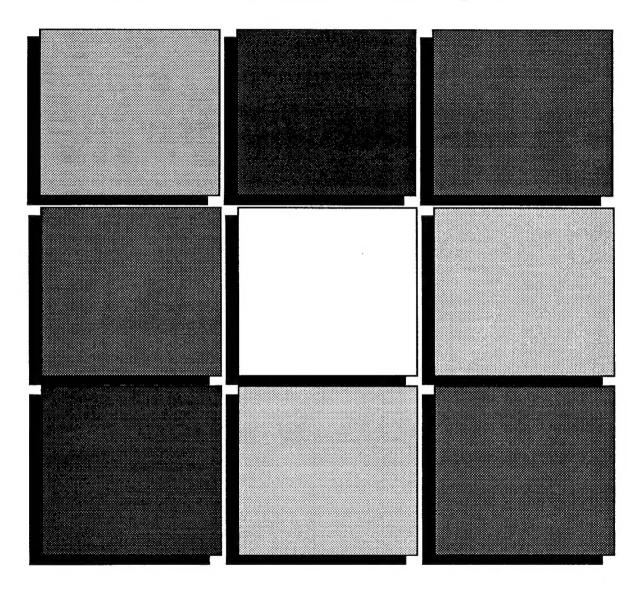
Software for Learning™

Award Winning Academic Learning Systems



(800) 336-1022 Sales and Information (805) 499-1407 Technical Support

(805) 498-8364 FAX Apple Link: VENTURA

Ventura Educational Systems

3440 Brokenhill Street Newbury Park, CA 91320

TO THE BOTTON OF STREET STREET

PROTECT MENTER OF THE SERVICE

organical and the end of the second

SuperGraph SuperGraph SuperGraph SuperGraph SuperGraph SuperGraph

A sophisticated tool for graphing complex mathematical relationships.
Built-in constants for solving problems in algebra, trigonometry, calculus and physics.
Includes a Teacher's Guide and reproducible blackline masters.
Program Disk and DataDisk with sample graphs.

© 1986 All Rights Reserved Ventura Educational Systems



Copyright Notice

This product is intended for use by individuals and schools. The purchaser is entitled to use this product but not to transfer or sell reproductions of the product or manual to other parties.

Apple Computer, Inc. makes no warranties, either express or implied, regarding the enclosed computer software package, its merchantability or its fitness for any particular purpose. The exclusion of implied warranties is not permitted by some states. The above exclusion may not apply to you. This warranty provides you with specific legal rights. There may be other rights that you may have which vary from state to state.

DOS 3.3 is a copyrighted program of Apple Computer, Inc. licensed to Ventura Educational Systems to distribute for use only in combination with Ventura Educational Systems Learning Software. Apple® software shall not be copied onto another diskette (except for archival purposes) or into memory unless as part of the execution of Ventura Educational Systems' Software for Learning. When the programs have completed execution Apple software shall not be used by any other program. Apple is the registered trademark of Apple Computer. Software for Learning products are copyrighted programs of Ventura Educational Systems.

This program is provided on a 5 1/4 inch floppy disk for use on Apple Computers. You are entitled to use this program on a single computer. A license is required for legal use of this program on a network or to make multiple copies of this program. Please contact Ventura Educational Systems directly for more information on software licensing and additional program disks.

Ventura Educational Systems 3440 Brokenhill Street Newbury Park, CA 91320

Contact to Same

(805)-499-1407

ι. .

SuperGraph

The ability to quickly graph complex mathematical relationships is a definite asset in studying algebra, trigonometry and calculus. SuperGraph is a software tool that allows relationships to be defined for f(x) and g(x). It unlocks the power of your computer to represent mathematical functions and can be very useful in mathematics classes.

Common functions are built-in features of SuperGraph and others can be defined by the user. The program internalizes any syntactically correct expression and generates a graph at lightening speed.

Credits

Software Design

Ventura Educational Systems

Concept and Programming

Dominick Cancilla

Editor

Fred Ventura, Ph.D.

Dominick Cancilla is a mathematics and programming specialist. In SuperGraph he has created a unique and creative tool for mathematics instructors and students who want an easy to use program that is able to represent complex mathematical relationships.

Dr. Fred Ventura is an experienced classroom teacher and has taught elementary, secondary and college levels. He holds a doctorate in education from the University of California, and presents workshops for educators on the instructional uses of microcomputers.

Other software products available from Ventura Educational Systems:

Hands-On Math

GeoArt: Geometry and Art Discovery Unit Marine Life: Anatomy of a Fish

Anatomy of a Sea Lamprey

Senses: Physiology of the Human Sense Organs

The Plant: Nature's Food Factory

Chemaid: Introduction to the Periodic Table

The Worm: Invertebrate Anatomy

Protozoa: Introduction to Microorganisms States: Geography Study Unit and Database All About the Solar System

All About Simple Machines

Dr. Know: Experiments in Artificial Intelligence

Coordinate Geometry Geometry Concepts Marine Invertebrates Anatomy of a Shark

> VisiFrog: Vertebrate Anatomy Computer Concepts Plant and Animal Cells The Insect World All About Matter All About Light & Sound



General Description

SuperGraph is designed to be a tool for teachers and students. The program allows the user to enter mathematical relationships, from simple linear equations, y=2*x+1, to complex functions, $y=\sin(x)*\cos(x^2)$, and see the curve produced by the equation graphed on the computer screen.

As students begin the study of higher mathematics they learn about vertically defined functions, f(x). Advanced mathematics students will appreciate the ability to define equations for both f(x) and g(x). Supergraph allows students to open the door to some very interesting graphs (see SuperGraph Demo) and this can provide a deeper insight into the mathematics.

Menu

After the title screen is displayed the SuperGraph menu will appear. The list below explains the functions that special keys have when the menu is active.

To add to the ease of use of SuperGraph several actions have been simplified to one or two key presses. Depending on where in the program the user is certain actions are available. The next section describes what key actions are available in different section of the program.

SuperGraph Main Menu and Demo

Kev Effect

arrows move indicator.

letter go to next item beginning with that letter.

<return> accept current setting or status.

<space> change columns in demonstration mode

or accept in other cases.

esc move to guit option.

Supergraph Reference

 Key
 Effect

 arrows
 move

 < and >
 page

 Q
 quit

 ? or H
 get help

-, = go to next, previous section

P print current level

<esc> go to previous section

Read/Write Option

<name>

read or write a SuperGraph data file

<name>.PIC

using the extension ".PIC" causes Supergrapher to read into or write from high resolution graphics

page 1

cat or dir

catalog the disk in drive #1 showing directory of files

Equation Editor

When defining an expression for either f(x) or g(x) the following keys are implemented to assist in editing. The definition of functions are stored in a buffer and can be moved in and out of the buffer using the arrow keys, delete and return.

Key	Effect
>	output from buffer
<	input to buffer
<delete></delete>	erase previous character
<return></return>	accept

In the equation editor several macros, key sequences that produce a function, are available. Macros are designed to simplify the entry of functions.

Macros Function CTRL-A ABS(CTRL-C COS(CTRL-D SGN(CTRL-E EXP(CTRL-F ATN(CTRL-I INT(CTRL-J SQR((down arrow) CTRL-K (up arrow)	, 4
CTDL 1	e a seementer
CTRL-O OR	- 1
CTRL-P PI	
CTRL-R RND(2 th 1 th
CTRL-S SIN(
CTRL-T TAN(* ***
CTRL-X AND	100

130

Same of the same



Using SuperGraph

SuperGraph is designed to encourage high-level mathematical exploration. The following operations, constants and functions are implemented in the program and can be used in defining expressions for f(x), and g(x). The SuperGraph Reference can be selected from the SuperGraph Menu and provides access to information on the operators, constants and functions available in SuperGraph.

Note: When using SuperGraph be sure that the Caps-Lock key on the Apple keyboard is depressed.

Operations		
Symbol		Example
+	addition	1+1
-	subtraction	1-1-2
*	multiplication	2*4
1	division	3/5
۸	exponentiation	3^2
=	equal	1=2-1
>	greater than	2>1
<	less than	1<2
#	not equal	1#2
Ë	scientific notation	5E3

Implemented Functions

The functions that are described in this section are implemented in SuperGraph. The sophisticated equation processor used in SuperGraph internalizes syntactically correct functions. The definition of the equation can contain any of the following mathematical functions.

Basic Functions

Function	Description	Example
abs	absolute value	abs(X)
atn	arctangent in radians	atn(X)
cos	cosine in radians	cos(X)
ехр	Euler's constant to the power of X	exp(x)
int	largest integer less than or equal to a value	int(x)
log	natural logarithm	log(x)
rnd	random number greater than or equal to zero and less than one	rnd(x)
sgn	-1 if the value is negative, 1 if the value is positive and 0 if the value is zero	sgn(x)
sin	sine in radians	sin(x)
sqr	square root	sqr(x)
tan	tangent in radians	tan(x)



Extended Functions

The extended functions listed below can used equations. Each function begins with the @ symbol.

Function	Description	Example	Formula
@arccos	inverse cosine	@arccos(x)	(-atn(x/sqr(-x^-2+1))+pi/2)
@arccosh	inverse hyper- bolic cosine	@arccosh(x)	$log(x+sqr(x^2-1))$
@arccot	inverse cotangent	@arccot(x)	(-atn(x)+pi/2)
@arccoth	inverse hyperbolic cotangent	@arccoth	log((x+1)/(x-1))/2
@arccsc	inverse cosecant	@arccsc(x)	(atn(1/sqr(x^2-1)+(sgn(x)-1)*pi/2)
@arccsch	inverse hyperbolic cosecant	@arccsch(x)	$\log(\operatorname{sgn}(x)^*\operatorname{sqr}(x+1)+1)/2$
@arcsec	inverse secant	@arcsec(x)	(atn(sqr(x^2-1))+(sgn(x)-1)*pi/2)
@arcsech	inverse hyperbolic secant	@arcsech(x)	$log(sqr(-x^2+1)+1/x)$
@arcsin	inverse sine	@arcsech(x)	atn(x/sqr(-x^2+1))
@arcsinh	inverse hyperbolic sine	@arcsinh(x)	log(x+sqr(x^2+1))
@arctanh	inverse hyperbolic tangent	@arctanh	log((1+x)/(1-x))/2
@cosh	hyperbolic cosine	@cosh(x)	$(\exp(x)+\exp(-x))/2$
@cot	cotangent	@cot(x)	1/tan(x)
@coth	hyperbolic cotangent	@coth(x)	(exp(-x)/(exp(x)-exp(-x))*2+1)
@csc	cosecant	@csc(x)	1/sin(x)
@csch	hyperbolic cosecant	@csch(x)	2/(exp(x)-exp(-x))

@log	base 10 log	@log(x)	log(x)/log(10)
@rnd	random number between 0 and the value of X	@rnd(x)	int(x*rnd(1))
@sec	secant	@sec(x)	1/cos(x)
@sech	hyperbolic secant	@sech(x)	(2/exp(x)+exp(-x)))
@sinh	hyperbolic sine	@sinh(x)	(exp(x)-exp(-x))/2
@tanh	hyperbolic tangent	@tanh(x)	(-exp(-x)/(exp(x)+exp(-x))*2+1)

Conversions

Conversions can be performed automatically by expressing the conversion as a function when using the equation editor.

Function	Description	Example	Formula
@D]G	converts from degrees to gradients	@DJG(x)	10*x/9
@D]R	converts from degrees to radians	@D]R(x)	Pi*x/180
@G]D	converts from gradients to degrees	@G]D(x)	.1*x
@GJR	converts from gradients to radians	@G]R(x)	E 1 124
@R]D	converts from radians to degrees	@R]D(x)	180*x/pi
@R]G	converts from radians to gradients	@R]G	200*x/pi

2524 12 31

. . . .



Built-in Constants

Several values frequently used as constants in formulas are provided as built-in constants. These constants are commonly used in solving problems.

С	speed of light in miles/second	186,282
CM	speed of light in meters/second	299,792,458
E	Euler's constant	2.71828182
EO	permativity constant	8.854E-12
EV	electron volt in joules	1.60218E-19
G	gravitational constant in feet	32
GM	gravitational constant in meters cubed per KG-second squared	6.672E-11
Н	Plank's constant in joules/second	6.626E-34
e personal and a second	Coulomb's constant in newton-meters squared per coulomb squared	8.988E9
KB	Boltsmann's constant	1.38066E-23

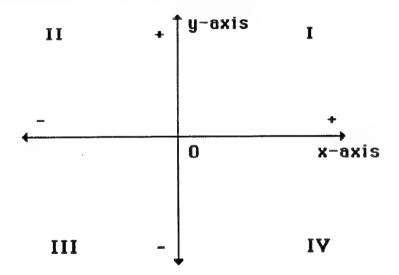
Error Messages

Illegal quantity
/0 (division by 0)
illegal file name (file not found, wrong disk)
disk full
I/O error (drive open, bad disk, no disk)
remove write protect tab (disk write protected)
syntax (illegal characters, mismatched parenthesis)

Coordinate Systems

Two straight lines drawn in the same plane and perpendicular to each other intersect at what is called the origin. The origin can be used to establish the relative position of points on the plane. These lines are called the axes. The horizontal axis is referred to as the x-axis and the vertical axis is called the y-axis. Any point can be defined using an abscissa (x-coordinate) and an ordinate (y-coordinate).

The axes divide the plane into four distinct regions which are called quadrants. The quadrants are labelled as shown.



Functions are the numerical dependence of one quantity on one or more other quantities. For example the area of a square is a function of the length of the side. In strict mathematical interpretations y is described as a function of x if there is a corresponding value relative to the y axis for each point on the x-axis. The notation y=f(x) is read y is equal to f of x. The x term is called the argument and is the independent variable. The dependent variable is the y-term since it depends on x.

x is said to vary continuously if it can take all the values in an interval, for example -1 and +1. The function y=f(x) is said to be continuous at a point x_0 in the given interval if as x approaches x_0 , y yields a finite value which is equal to $f(x_0)$.

Graphs are an excellent way to represent a continuous function where a single independent variable is used to produce a curve. Graphs provide insight into the relationship of y and x.

3117



SuperGraph Options

Each graph produced by SuperGraph can be defined using these options:

Ticks Ticks are the tiny marks that appear on the x and y axes.

The ticks are used to help determine values of points on the line that is plotted. The value that is set for ticks determines how many marks for each unit. The size of the unit is set by

the Scale option.

The scale of the graph is determined by the setting given to Scale

this variable. Each dot on the computer screen is called a pixel. The scale setting determines how many pixels define one unit. If the scale is 10 then 1 unit on the graph is 10

pixels.

First X Last X

First X and Last X are used to define the domain for the graph. The domain is set of numbers between lowest x

value and the highest x value.

The accuracy factor is a percentage value that determines Accuracy

how many points are used to define the graph.

Pre-define The Pre-define option controls whether or not the

coordinates are displayed or printed before the graph is

drawn.

Noise The Noise option controls whether the computer produces a

click when each point is plotted.

Color Set The Color Set option determines how the graph looks. If

the color set is white the graph is drawn in white on a black background. If the color set is switched to black, then the

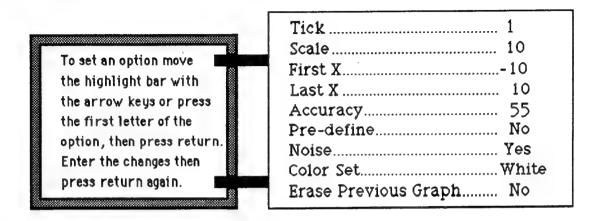
graph is drawn with black on a white background.

Erase Previous Graph

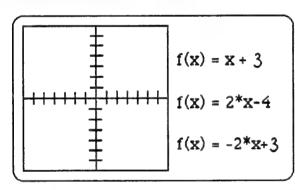
In the study of mathematics it is often desirable to plot more than one function on the same grid. This option is used to control whether the screen is erased before a function is

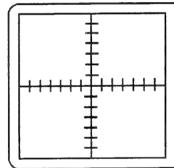
plotted.

For the activities on this page set up the SuperGraph options as shown:



Set the Vertical Equation for the functions shown and sketch the graph produced by each function.



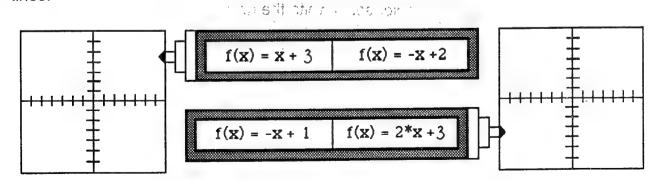


$$f(x) = \frac{1}{2} * x - 3$$

$$f(x) = 2 * x + 4$$

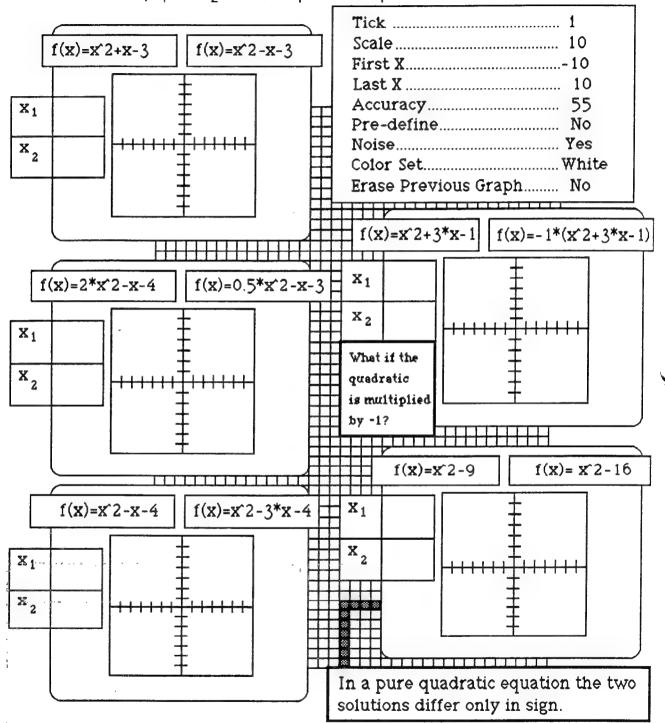
$$f(x) = -2 * x - 1$$

Use SuperGraph to find the points of intersection for each of these pairs of lines:

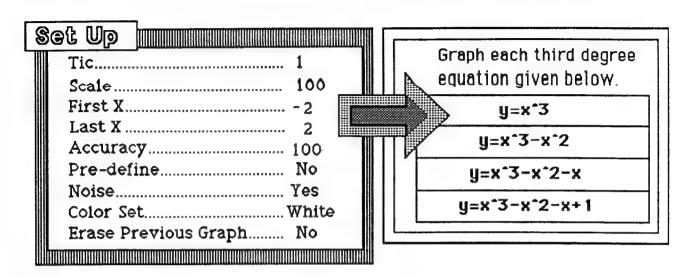


2nd degree (quadractic equations)

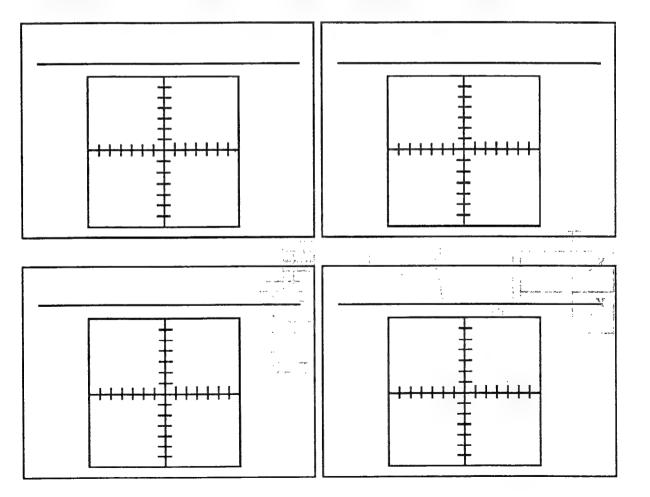
Write the solutions, x_1 and x_2 for these quadratic equations:



3rd degree (cubic equations)



Using the set up given above plot these curves with SuperGraph. Write the function on the line and sketch the curves on the graphs given below.



Use this setup to plot these 4th degree equations:

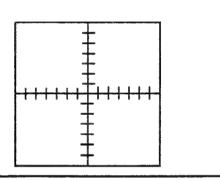
Tic	1
Scale	10
First X	10
Last X	10
Accuracy	70
Pre-define	No
Noise	Yes
Color Set	White
Erase Previous Graph	No

$$x^4 - x^3 + 2x^2 - x + 1 = 0$$

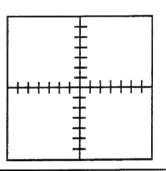
4th degree equations are called biquadratic equations.

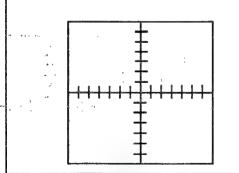
Use SuperGraph to plot these equations. Sketch the results.

$$y = x^4 - 3 * x^3 + x^2 + x - 1$$

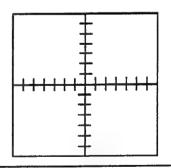


$$y = x^4 - 2 * x^3 + x^2 + x - 4$$





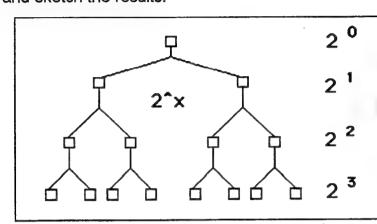
$$y = 3*x^4 - 2 * x^3 - x^2 - x - 1$$

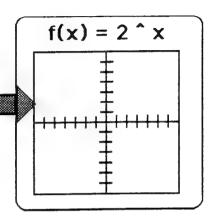


Combine the terms in these equations and graph the results.

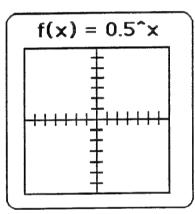
transcendental equations: exponential

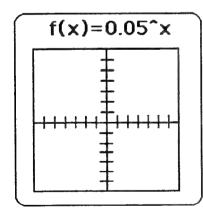
Algebraic equations which contain transcendental functions of the unknown are called transcendental equations. Graph these equations using SuperGraph and sketch the results.

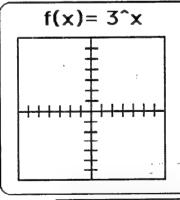


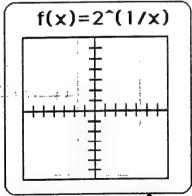


Tic	1
Scale	10
First X	0
Last X	4
Accuracy	55
Pre-define	No
Noise	Yes
Color Set	White
Erase Previous Graph	Yes







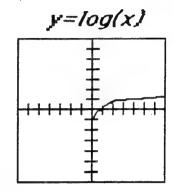


Set first x to 0.01 in order to avoid division by 0 error

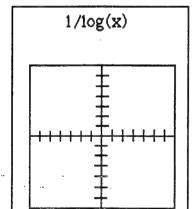
transcendental equations: logarithmic

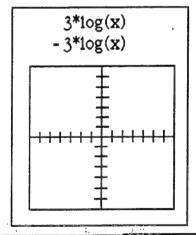
The SuperGraph equation processor has two logarithmic functions, LOG(X) and @LOG(X). The LOG(X) function returns the natural logarithm and the @LOG(X) function returns the base 10 log.

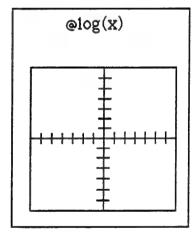
Tic	1
Scale	10
First X	0.1
Last X	20
Accuracy	55
Pre-define	No
Noise	Yes
Color Set	White
Erase Previous Graph	Yes

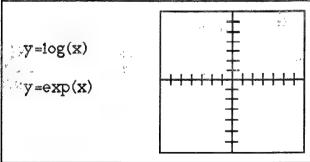


Use SuperGraph to sketch the graph of these logarithmic functions. Set the First X option to 1.1



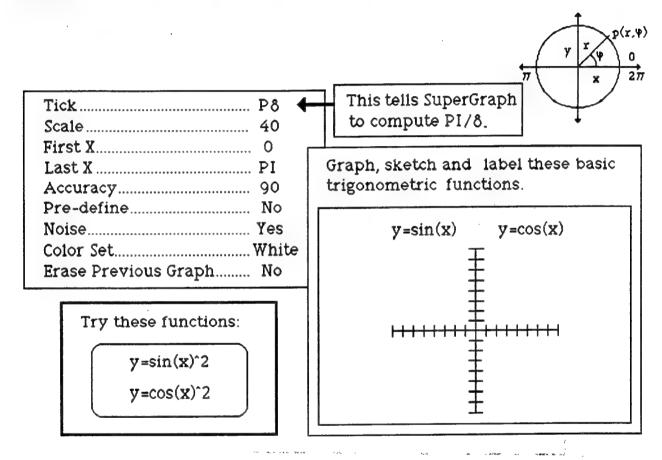






The natural logarithm $f(x)=\log(x)$ is defined as the inverse of the exponent function. Graph the natural log and the exponent function for all values of x between .1 and 10. Sketch the graph in the box to the left.

SuperGraph has the capability to graph several trigonometric functions. These exercises introduce the trigonometric functions, but a great deal can be learned by experimenting. Trigonometric functions return values in radians. The result of a trigonometric function can be converted to degrees using the @R]D(x) function.



SuperGraph can be used to solve equations. Here is an example:

$$\frac{1}{x} - \frac{2}{3} = \sin(x)$$

To graphically solve this equation, first plot the sine function using SIN(X). Next plot the function Y=X-(2/3)*PI. Observe the point on the graph where the sine curve and the line cross. The x-coordinate of this point is approximately 2.6. the solution!

SuperGraph has the basic trigonometric functions, sine, cosine and tangent, but can also accept most other trigonometric functions. Try these experiments which use some of the special trigonometric functions.

 Tick
 1

 Scale
 20

 First X
 -PI

 Last X
 PI

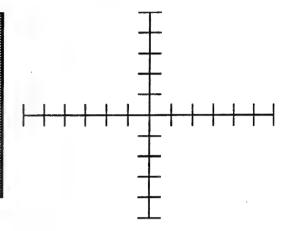
 Accuracy
 90

 Pre-define
 No

 Noise
 Yes

 Color Set
 White

 Erase Previous Graph
 No

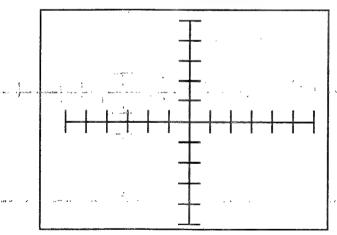


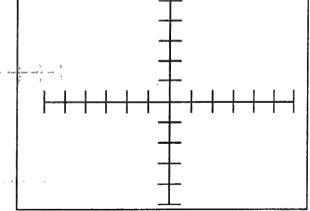
Sketch the curve produced by these function:

- f(x) = @ARCCOS(X)
- inverse cosine
- f(x) = @ARCCOT(X)
- inverse cotangent
- f(x) = @ARCSIN(X)
- inverse sine

For these functions set the first x to .01 and the last x to pi (3.14)

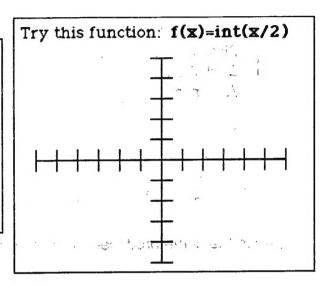
- f(x) = @COSH(X)
- f(x) = CSC(X)
- f(x) = @COSH(X)
- f(x) = CSCH(X)



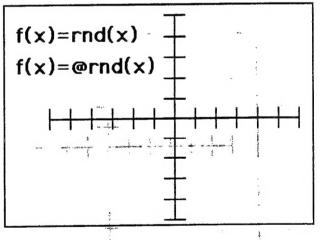


The integer function, int(x) returns the largest integer less than or equal to the value within the parentheses.

Tick	1
Scale	20
First X	-10
Last X	10
Accuracy	90
Pre-define	No
Noise	Yes
Color Set	White
Erase Previous Graph	No

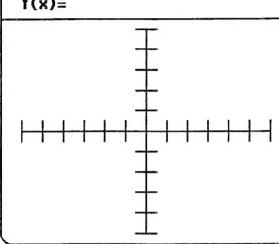


On the left use SuperGraph to overlay the square root function, SQR(X) on a graph of X^2. Set the first x to 0 to avoid an error by trying to compute the square root of a negative number. On the right use SuperGraph's built in random functions. The RND(X) function returns a value greater than 0 and less than 1. The @RND(X) returns a value between zero (0) and the number (x).

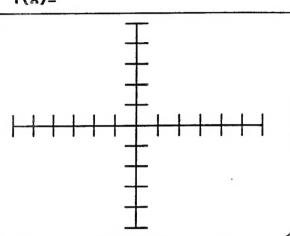


explorations

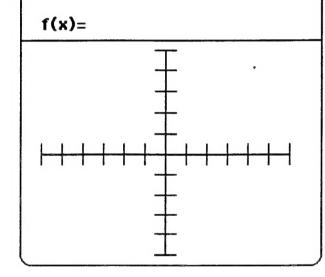
$$f(x)=$$

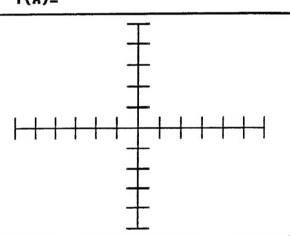


$$f(x)=$$



$$g(x)=$$





SGN ABS ATN SIN

cos SQR **EXP** TAN INT

@ARCCOS LOG @ARCCOSH RND @ARCCOT

@ARCCOTH @ARCCSC

@ARCCSCH @ARCSEC @ARCSECH @ARCSINH

@ARCTANH

@COSH @COT

@COTH @CSC @LOG

@RND @SEC

@SECH

@SINH @TANH

@DIG @DJR @GID

@R]D @R]G

Software Order Form

Ship to:

Name

Try these academic learning programs in your classroom.

To order by phone call: (800) 336-1022

Check one:

Bill me (school address

School				required). Shipping and handling is extra.		
School Address		1		;		
City State ZIP				Send programs listed below. Purchase order		
Bill to:		ř 3		is enclosed		
Name						
School			If you are not completely satisfied			
School Address				you may return the program in good condition within 30 days for		
City State	ZIP			or cancellation		
Title and Format	Single	Lab-Pack	Quantity	Price	Amount	
THO GITO I DITTING	- James				7	
		1 .				
· ·			, .		,	
			ı		7	
				,		
		1 6				
:			VIA (802)			
	F shipedata an		ا ما المحافظ الما المحافظ الما المحافظ	and the state of t	er or manuscript	
Send your completed order	to:			Subtotal		
	17%-italiq ci-atur	Blancon (Marie Consulting of Marie of Marie (Marie Marie)	N'INDEED A. S.	Tax (in CA)	en kow-re se	
			. 19 5-5			
			7. 3.	Total	<u> </u>	
	ĝ,			MAT SI	5	
Ve1	ıtura	Educ	ation	il Sus	tems	
		- 100 A A				
★ 3440 Bi	rokenhill Str	eet * New	rbury Park, CA	\ 913 2 0 ***	799	

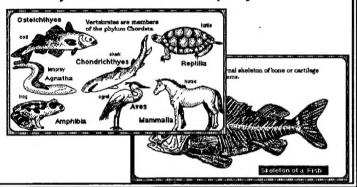
New Software Titles from Ventura Educational Systems

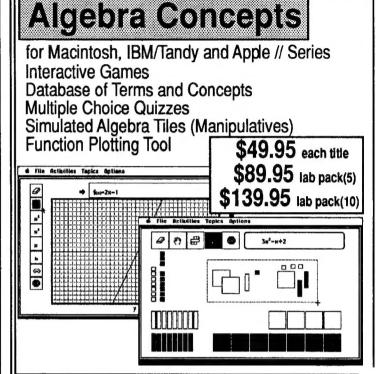
Marine Life Series

Now available for Macintosh, IBM/Tandy and Apple // Series

Marine Invertebrates
Anatomy of a Shark
Anatomy of a Fish
Life Cycle of a Sea Lamprey

\$49.95 each title \$89.95 lab pack(5) \$139.95 lab pack(10)







The Hands-On **Math Series** Computer Simulated Math Manipulatives Volume 3 11 12 13. Volume 1 Volume 2 21 22 23 Rods Two-Color Counters Hundreds Chart **Number Tiles Color Tiles** Graphing Counters Mirrors **Number Balance** Chip-Trading Attribute Blocks **Dominoes** Geoboard Base Ten Blocks Line Design Tangrams **Fraction Bars** \$49.95 each Volume 1 available for Apple, volume Macintosh and IBM/Tandy Volumes 2 and 3 for Apple only.

To Order Call:

(800) 336-1022



Information: (805) 499-1407 FAX: (805) 498-8364 Apple Link: VENTURA

Ventura Educational Systems